QQPlots in GWAS

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QQ Plots and GWAS

- Purpose: Determine if there are a likely a large number of false positive in the GWAS
- Method: Compare the p-values from the GWAS to those expected from doing the same number of SNP tests if there were no true associations.
- Logic: Only a very, very small number of SNPs should be associated with our trait.
- Therefore, the distribution of p-values obtained from the true GWAS should mostly match those from random data.

What is QQ anyway?

- · Q-Q stands for quantile-quantile
- OK so what is a quantile?
- You are probably familiar with percentiles.
- Quantiles are similar but are cut points that divide a set of observations (or a distribution) into evenly sized groups.
- For example, quartiles divide a set of observations into 4 groups, split at the 25th, 50th, and 75th percentile.
- · An example may help:

Quantiles example

```
somedata <- rnorm(n=20, mean=10, sd=3) %>% sort()
somedata

## [1] 3.355900 7.493114 7.538595 8.120639 8.136278 9.083835 9.865199
## [8] 9.951429 10.550930 10.988523 11.169530 11.462287 11.727344 11.781704
## [15] 12.214974 12.463664 12.831509 13.374793 14.535344 14.785842

quantile(somedata, c(.25,.5,.75))

## 25% 50% 75%
## 8.846946 11.079027 12.277146
```

- the 25% quantile is between the 5th and 6th data point
- the 50% is between the 10th and 11th
- and the 75% is between 15th and 16th

What are expected p-values?

- · Expected p-values are those we would expect to see in a randomized data set.
- These are simple to calculate. If we had a 100 randomized data sets (or SNPs), then:
- We expect 1 test (1%) to have a p-value of <= 0.01
- We expect 5 tests (5%) to have a p-value of <= 0.05
- We expect 75 tests (75%) to have a p-value of <= 0.75
- · Thus if you know the quantile, you know the expected p-value!

But how does this work in practice?

GWAS with 10 SNPs:

```
## # A tibble: 100 x 12
##
          plantID height SNP1
                                                SNP2 SNP3
                                                                                             SNP6
                                                                                                        SNP7
                                                                       SNP4
                                                                                  SNP5
                                                                                                                   SNP8
                                                                                                                              SNP9
                                                                                                                                         SNP10
##
              <int> <dbl> <chr> <chr
##
                           10.8
                                                 C
                                                                                  C
                                                                                             G
                                                                                                        G
                                                                                                                              C
                                                                                                                                         C
                                                            A
                                                                       Α
                                                                                                                   T
       1
##
       2
                           11.6
                                                 C
                                                            G
                                                                                  C
                                                                                             C
                                                                                                        C
                                                                                                                              \mathbf{T}
                                                                                                                                         C
##
       3
                             9.15 G
                                                 Т
                                                                       Τ
                                                                                  G
                                                                                             C
                                                                                                        C
                                                                                                                             C
                                                                                                                                        G
                                                            Α
##
       4
                             6.02 T
                                                                                  C
                                                                                             C
                                                                                                        C
                                                            G
                                                                                                                  C
                                                                                                                                        G
                                                                       Α
##
       5
                     5 10.2 G
                                                 C
                                                            Α
                                                                                  C
                                                                                             C
                                                                                                        C
                                                                                                                                        G
                                                                       Α
##
                             9.89 T
                                                 C
                                                            G
                                                                                             G
                                                                                                                                         C
##
                             8.69 G
                                                                                             C
                                                            A
                                                                                                                                         C
##
                             7.06 T
                                                            G
                                                                                             G
                                                                                                        G
                                                                                                                                         C
                                                 C
##
                     9
                             8.04 G
                                                                                             C
                                                                                                        C
                                                                                                                             C
                                                                                                                                        C
       9
                                                            A
                                                                       Α
## 10
                                                            G
                                                                                  G
                                                                                             C
                                                                                                        C
                                                                                                                   C
                                                                                                                                         C
                    10
                           10.8 T
                                                 C
                                                                                                                              \mathbf{T}
## # ... with 90 more rows
```

Test association for each SNP and get pvalue

First: pivot to longer

```
snplong <- snpdata %>%
 pivot longer(c(-plantID, -height), names to="SNP name", values to = "genotype") %>%
  arrange(SNP name)
snplong
## # A tibble: 1,000 x 4
##
     plantID height SNP name genotype
       <int> <dbl> <chr>
##
                            <chr>
##
           1 10.8 SNP1
   1
                            G
## 2
           2 11.6
                    SNP1
## 3
           3 9.15 SNP1
                            G
## 4
           4 6.02 SNP1
## 5
           5 10.2 SNP1
## 6
           6 9.89 SNP1
## 7
           7 8.69 SNP1
##
           8 7.06 SNP1
##
   9
           9 8.04 SNP1
## 10
          10 10.8 SNP1
## # ... with 990 more rows
```

Next do a t-test on each SNP and extract p value

```
pvals <- snplong %>% group by(SNP name) %>%
 summarize(gwas pval=t.test(height ~ genotype)$p.value)
pvals
## # A tibble: 10 x 2
     SNP name gwas pval
      <chr>
                  <dbl>
## 1 SNP1
                 0.862
## 2 SNP10
                 0.455
## 3 SNP2
                 0.379
## 4 SNP3
                 0.0195
  5 SNP4
                 0.170
## 6 SNP5
                 0.691
## 7 SNP6
                 0.610
## 8 SNP7
                 0.859
## 9 SNP8
                 0.483
## 10 SNP9
                 0.0238
```

These are the **observed** pvalues

sort based on p-value, add quantile

For these type of plots often we calculate a quantile for every test.

```
pvals <- pvals %>%
  arrange(gwas pval) %>%
 mutate(quantile=1:nrow(pvals)/nrow(pvals))
pvals
## # A tibble: 10 x 3
##
      SNP name gwas pval quantile
##
      <chr>
                   <dbl>
                            <dbl>
   1 SNP3
                  0.0195
                              0.1
##
                  0.0238
##
   2 SNP9
                              0.2
##
                              0.3
   3 SNP4
                0.170
##
   4 SNP2
                  0.379
                              0.4
                              0.5
##
   5 SNP10
                  0.455
                  0.483
                              0.6
##
    6 SNP8
##
   7 SNP6
                  0.610
                              0.7
    8 SNP5
                  0.691
                              0.8
                  0.859
                              0.9
   9 SNP7
## 10 SNP1
                  0.862
                              1
```

calculate expected p values, convert to -log10(p)

```
pvals <- pvals %>%
  mutate(exp pval = quantile,
         neglog10 \text{ gwas} = -log10(\text{gwas pval}),
         neglog10 expected = -log10(exp pval))
pvals
## # A tibble: 10 x 6
##
      SNP name gwas pval quantile exp pval neglog10 gwas neglog10 expected
##
                    <dbl>
                                       <dbl>
                                                     <dbl>
      <chr>
                             <dbl>
                                                                        <dbl>
    1 SNP3
                   0.0195
                               0.1
                                         0.1
                                                    1.71
##
                                                                        1
##
    2 SNP9
                  0.0238
                               0.2
                                         0.2
                                                    1.62
                                                                       0.699
                               0.3
                                         0.3
                                                    0.770
##
    3 SNP4
                  0.170
                                                                       0.523
##
    4 SNP2
                  0.379
                               0.4
                                         0.4
                                                    0.421
                                                                       0.398
##
    5 SNP10
                  0.455
                               0.5
                                         0.5
                                                    0.342
                                                                       0.301
                                         0.6
                                                                       0.222
    6 SNP8
                  0.483
                               0.6
                                                    0.316
    7 SNP6
                  0.610
                               0.7
                                         0.7
                                                    0.215
                                                                       0.155
##
    8 SNP5
                  0.691
                               0.8
                                         0.8
                                                    0.160
                                                                       0.0969
    9 SNP7
                  0.859
                               0.9
                                         0.9
                                                    0.0662
                                                                       0.0458
## 10 SNP1
                   0.862
                               1
                                                    0.0646
                                         1
                                                                        0
```

plot it

